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# The Basic Building Blocks of NMR Pulse Sequences

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#### Introduction and outline

- most pulse sequences are built up from simpler elements or building blocks – of which there are not that many
- recognising these elements can help in understanding how a pulse sequence 'works', and will usually simplify a detailed analysis
- new pulse sequences are often designed by joining together these building blocks
- a PDF of this presentation is available to download at www-keeler.ch.cam.ac.uk

Introduction and outline 2

#### Introduction and outline

- we will restrict ourselves to building blocks used in liquid-state NMR for scalar coupled spins systems
- everything will be illustrated for two coupled spins one-half
- we will start with a brief reminder of the product operator method, as this will be used to describe each building block
- and then go on to cover as many buildings blocks as time permits
- for more detail: James Keeler, Understanding NMR Spectroscopy, 2nd edit., Wiley 2010

#### Building blocks to be covered

- 1. Product operators
- 2. Decoupling
- 3. Spin echoes
- 4. Heteronuclear coherence transfer using INEPT
- 5. Heteronuclear coherence transfer using HMQC
- 6. Generation and detection of multiple-quantum coherence
- 7. Constant time sequences
- 8. Isotropic mixing (TOCSY)
- 9. z-filters
- 10. Gradient echoes
- 11. Spin locking

## Product operators

- ► the state of the spin system can be expressed in terms the nuclear-spin angular momentum operators  $\hat{I}_x$ ,  $\hat{I}_y$ , and  $\hat{I}_z$
- Î<sub>x</sub>, Î<sub>y</sub>, and Î<sub>z</sub> represent the x-, y- and z-components of the magnetization
- can just 'read off' the expected magnetization
- equilibrium magnetization only along z:  $\hat{I}_z$

Product operators 6

#### Evolution

- evolution depends on the relevant Hamiltonian
- free precession:

 $\hat{H}_{\text{free}} = \Omega \hat{I}_z$ 

 $\Omega$  is the offset in the rotating frame

hard pulse about x-axis:

$$\hat{H}_{x,\text{hard pulse}} = \omega_1 \hat{I}_x$$

- $\omega_1$  is the RF field strength
- hard pulse about y-axis:

$$\hat{H}_{y,\text{hard pulse}} = \omega_1 \hat{I}_y$$

#### Arrow notation

write 'Hamiltonian × time' over the arrow

initial state  $\xrightarrow{\text{Hamiltonian} \times \text{time}}$  final state

for example, pulse of duration t<sub>p</sub> about x to equilibrium (z-) magnetization

$$\hat{I}_z \xrightarrow{\omega_1 t_p \hat{I}_x}$$
 final state

• but  $\omega_1 t_p$  is the flip angle  $\beta$ 

$$\hat{I}_z \xrightarrow{\beta \hat{I}_x}$$
 final state

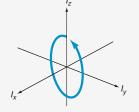
► for example, free evolution of *x*-magnetization for time *t* 

$$\hat{I}_x \xrightarrow{\Omega t \hat{I}_z}$$
 final state

Product operators 5

#### Diagrammatic representation of rotations

- in general the rotation of an operator  $\hat{A}$  gives two terms:
  - 1.  $\hat{A}$  multiplied by the cosine of an angle
  - 2. a 'new' operator,  $\hat{B}$ , multiplied by the sine of the same angle
- $\cos\theta \times \text{original operator} + \sin\theta \times \text{new operator}$
- can work out what the 'new operator' is by looking at the diagram

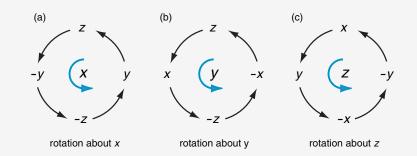


Product operators 9

#### Operators for two spins

description	operator(s)
z-magnetization on spin 1	$\hat{I}_{1z}$
in-phase x- and y-magnetization on spin 1	$\hat{I}_{1x}, \hat{I}_{1y}$
z-magnetization on spin 2	$\hat{I}_{2z}$
in-phase x- and y-magnetization on spin 2	$\hat{I}_{2x}, \hat{I}_{2y}$
anti-phase x- and y-magnetization on spin 1	$2\hat{I}_{1x}\hat{I}_{2z}, 2\hat{I}_{1y}\hat{I}_{2z}$
anti-phase x- and y-magnetization on spin 2	$2\hat{I}_{1z}\hat{I}_{2x}, 2\hat{I}_{1z}\hat{I}_{2y}$
multiple-quantum coherence	$2\hat{I}_{1x}\hat{I}_{2x}, 2\hat{I}_{1x}\hat{I}_{2y}, 2\hat{I}_{1y}\hat{I}_{2x}, 2\hat{I}_{1y}\hat{I}_{2y}$
non-equilibrium population	$2\hat{I}_{1z}\hat{I}_{2z}$

#### Diagrammatic representation of rotations



can be used to determine the effect of any rotation

 $\cos\theta \times \text{original operator} + \sin\theta \times \text{new operator}$ 

 $90^\circ$  or  $180^\circ$  rotations particularly simple: just move one or two steps around the clock

#### Product operators 10

#### Generation of anti-phase terms by evolution of coupling

- Hamiltonian for coupling:  $2\pi J_{12}\hat{I}_{1z}\hat{I}_{2z}$
- evolution of  $\hat{I}_{1x}$  under coupling from time  $\tau$

 $\hat{I}_{1x} \xrightarrow{2\pi J_{12}\tau \hat{I}_{1z}\hat{I}_{2z}} \cos\left(\pi J_{12}\tau\right) \hat{I}_{1x} + \sin\left(\pi J_{12}\tau\right) 2\hat{I}_{1y}\hat{I}_{2z}$ 

- evolution of *in-phase* (along *x*) to *anti-phase* (along *y*) magnetization
- complete conversion to anti-phase when  $\tau = 1/(2J_{12})$

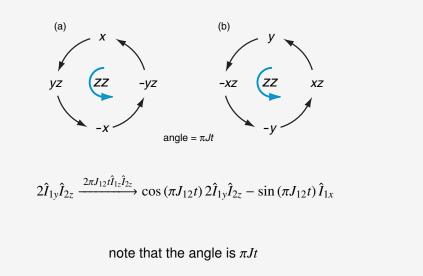
#### Anti-phase terms evolve back into in-phase terms

#### Diagrammatic representation: evolution of coupling

• evolution of  $2\hat{I}_{1y}\hat{I}_{2z}$  under coupling from time  $\tau$ 

$$2\hat{I}_{1y}\hat{I}_{2z} \xrightarrow{2\pi J_{12}\tau\hat{I}_{1z}\hat{I}_{2z}} \cos(\pi J_{12}\tau) 2\hat{I}_{1y}\hat{I}_{2z} - \sin(\pi J_{12}\tau) \hat{I}_{1x}$$

- complete conversion to in-phase when  $\tau = 1/(2J_{12})$
- note anti-phase along y goes to in-phase along -x



Product operators 13

#### Coherence transfer

- an absolutely key concept in multiple-pulse NMR
- achieved by applying 90° pulse to anti-phase term

$$\underbrace{2\hat{l}_{1y}\hat{l}_{2z}}_{\text{on spin 1}} \xrightarrow{(\pi/2)\hat{l}_{1x}} 2\hat{l}_{1z}\hat{l}_{2z} \xrightarrow{(\pi/2)\hat{l}_{2x}} \underbrace{-2\hat{l}_{1z}\hat{l}_{2y}}_{\text{on spin 2}}$$

- only anti-phase terms are transferred
- anti-phase terms arise due to the evolution of coupling

## Decoupling



Product operators 14

- a broad-band decoupling sequence applied to the *I* spins effectively sets all heteronuclear couplings to the *S*-spins to zero
- the following are likely to be dephased:
  - 1. *I*-spin coherences (including heteronuclear multiple quantum)
  - 2. anti-phase terms on *I* (e.g.  $2\hat{I}_z\hat{S}_x$ )
  - 3. z-magnetization on I
- unless decoupling only applied for a short period
- broad-band sequences gives decoupling over wide range of *I*-spin shifts with minimum of power, but there are practical limits to the range that can be covered

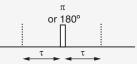
Decoupling 17

# Spin echoes

- by deliberately reducing the RF power level it is possible to restrict the decoupling effect to a narrower range of shifts
- e.g. decoupling of only the carbonyl carbons, or the  $\alpha$ -carbons
- only likely to be successful for a group of resonances which is well-separated from others

Decoupling 18





• start with  $\hat{I}_x$ 

$$\hat{I}_x \xrightarrow{\Omega \tau \hat{I}_z} \cos{(\Omega \tau)} \hat{I}_x + \sin{(\Omega \tau)} \hat{I}_y$$

• 180° pulse about x does not affect  $\hat{I}_x$ , and inverts  $\hat{I}_y$ 

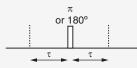
$$\cos{(\Omega\tau)\hat{I}_x} + \sin{(\Omega\tau)\hat{I}_y} \xrightarrow{\pi\hat{I}_x} \cos{(\Omega\tau)\hat{I}_x} - \sin{(\Omega\tau)\hat{I}_y}$$

second delay

$$\cos(\Omega\tau)\hat{I}_x - \sin(\Omega\tau)\hat{I}_y \xrightarrow{\Omega\tau\hat{I}_z} \cos(\Omega\tau)\cos(\Omega\tau)\hat{I}_x + \sin(\Omega\tau)\cos(\Omega\tau)\hat{I}_y - \cos(\Omega\tau)\sin(\Omega\tau)\hat{I}_y + \sin(\Omega\tau)\sin(\Omega\tau)\hat{I}_y$$

 $\equiv \hat{I}_r$ 

#### Spin echo for one spin



evolution between the dashed lines is

 $\hat{I}_x \xrightarrow{\tau - \pi - \tau} \hat{I}_x$ 

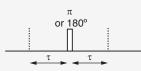
- the offset is said to be refocused between the dashed lines i.e. it is as if the offset (or the delay) is zero
- works just as well with other initial states
- in fact  $\tau \pi \tau \equiv \pi$

Spin echoes 21

#### Spin echo for (homonuclear) coupled spins

- ► a spin echo is *equivalent* to
  - 1. evolution of the coupling for time  $2\tau$
  - 2. followed by a 180° pulse (here about *x*).
- this is a very useful short cut in calculations
- key thing about a spin echo is that it enables us to interconvert in-phase and anti-phase magnetization in a way which is independent of the offset i.e. works for all spins

#### Spin echo for (homonuclear) coupled spins



- start with  $\hat{I}_{1x}$  and assume that offset is refocused
- the 180° pulse affects both spins ....
- ... final result is

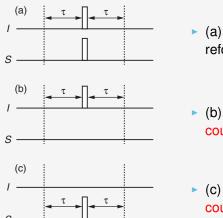
 $\cos{(2\pi J_{12}\tau)\hat{I}_{1x}} + \sin{(2\pi J_{12}\tau)}\hat{I}_{1y}\hat{I}_{2z}$ 

 coupling is not refocused, but continues to evolve for the entire period 2τ

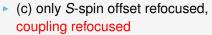
Spin echoes 22

#### Spin echoes in heteronuclear spin systems

can choose which spins to apply 180° pulses to



- (a) offsets refocused, coupling not refocused (as homonuclear)
- (b) only *I*-spin offset refocused, coupling refocused

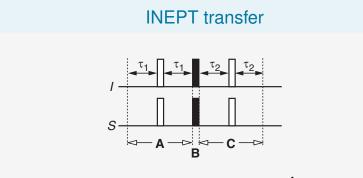


gives considerable flexibility

#### Spin echoes: summary

- in homonuclear systems spin echoes allow the coupling to evolve while effectively suppressing the evolution due to the offset (shift)
- means that we can interconvert in-phase and anti-phase terms in a way which is *independent of the offset*
- in heteronuclear systems spin echoes can effectively suppress the evolution of heteronuclear couplings, which is equivalent to 'decoupling', independent of offset

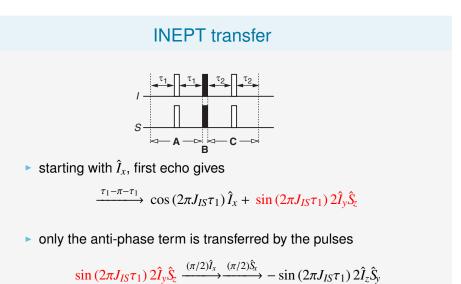
Spin echoes 25



- start with in-phase magnetization on I e.g.  $\hat{I}_x$
- anti-phase generated during spin echo A (independent of offset)
- coherence transfer from I to S during pulses B
- transferred anti-phase goes in-phase during spin echo C (independent of offset)
- overall result is transfer of in-phase on I to in-phase on S

# Heteronuclear coherence transfer using INEPT

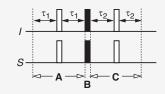
Heteronuclear coherence transfer using INEPT 26



anti-phase term goes in-phase during second spin echo

$$\xrightarrow{\tau_2 - \pi - \tau_2} \sin\left(2\pi J_{IS}\tau_2\right) \sin\left(2\pi J_{IS}\tau_1\right) \hat{S}_{A}$$

#### **INEPT** transfer



overall result is

$$\hat{I}_x \xrightarrow{\text{INEPT}} \sin(2\pi J_{IS}\tau_2) \sin(2\pi J_{IS}\tau_1) \hat{S}_x$$

- maximum transfer when  $\tau_1 = 1/(4J_{IS})$  and  $\tau_2 = 1/(4J_{IS})$
- if anti-phase term present at start of A, can omit first spin echo
- ► phase of 90° pulse to *I* affects which term is transferred i.e.  $2\hat{I}_y\hat{S}_z$  or  $2\hat{I}_x\hat{S}_z$

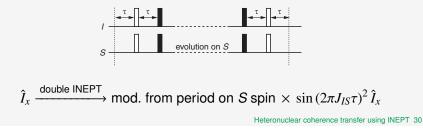
Heteronuclear coherence transfer using INEPT 29

#### Double INEPT transfer

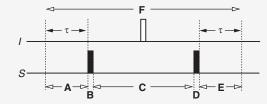
transfer from I to S; evolution; transfer back from S to I



- $\hat{I}_x \xrightarrow{\text{double INEPT}} \text{mod. from period on } S \operatorname{spin} \times \sin(2\pi J_{IS}\tau)^4 \hat{I}_x$
- can omit middle two spin echoes if evolution of an anti-phase term is acceptable



#### Coherence transfer using heteronuclear multiple quantum

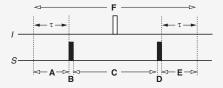


- rather like double INEPT
- *I*-spin offset refocused over whole of period F (spin echo due to central 180° pulse)
- start with  $\hat{I}_x$ : goes anti-phase during  $\tau$  to give  $\sin(\pi J_{IS}\tau) 2\hat{I}_y \hat{S}_z$
- S-spin 90° pulse transfers this to heteronuclear multiple-quantum coherence (HMQC)

$$\sin(\pi J_{IS}\tau) \, 2\hat{I}_y \hat{S}_z \xrightarrow{(\pi/2)\hat{S}_x} - \sin(\pi J_{IS}\tau) \, 2\hat{I}_y \hat{S}_y$$

# Heteronuclear coherence transfer using HMQC

#### Coherence transfer using HMQC



- HMQC does not evolve under J<sub>IS</sub>; I-spin offset also refocused
- evolution under just S-spin offset for period C

 $-\cos\left(\Omega_{S}t\right)\sin\left(\pi J_{IS}\tau\right)\hat{2I}_{y}\hat{S}_{y}+\sin\left(\Omega_{S}t\right)\sin\left(\pi J_{IS}\tau\right)\hat{2I}_{y}\hat{S}_{x}$ 

▶ 90° pulse to *S* transfers only the first term to give

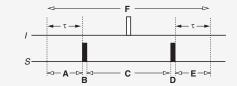
 $-\cos\left(\Omega_{S}t\right)\sin\left(\pi J_{IS}\tau\right)2\hat{I}_{y}\hat{S}_{z}$ 

 $\blacktriangleright$  this goes in-phase during the final delay  $\tau$  to give

 $\cos\left(\Omega_{S}t\right)\sin\left(\pi J_{IS}\tau\right)\sin\left(\pi J_{IS}\tau\right)\hat{I}_{x}$ 

Heteronuclear coherence transfer using HMQC 33

#### Coherence transfer using HMQC



net result is

 $\hat{I}_x \xrightarrow{\text{HMQC transfer}} \text{mod. from } S\text{-spin} \times \sin^2(\pi J_{IS}\tau) \hat{I}_x$ 

- optimum delay  $\tau$  is  $1/(2J_{IS})$
- similar to double INEPT

Heteronuclear coherence transfer using HMQC 34

#### Generation of multiple quantum coherence (MQC)

simply:

$$\underbrace{2\hat{I}_{1x}\hat{I}_{2z}}_{\text{anti-phase on spin 1}} \xrightarrow{(\pi/2)(\hat{I}_{1x}+\hat{I}_{2x})} \underbrace{-2\hat{I}_{1x}\hat{I}_{2y}}_{\text{MQC}}$$

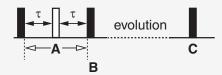
- only anti-phase terms are converted to MQC
- MQC not directly observable, but can be transferred back to anti-phase with a further pulse

 $2\hat{I}_{1x}\hat{I}_{2y} \xrightarrow{\text{evolution of offset}}$ mixture of terms:  $2\hat{I}_{1x}\hat{I}_{2y}$ ,  $2\hat{I}_{1y}\hat{I}_{2y}$ ,  $2\hat{I}_{1x}\hat{I}_{2x}$ ,  $2\hat{I}_{1y}\hat{I}_{2x}$ 

• only  $2\hat{I}_{1x}\hat{I}_{2y}$  and  $2\hat{I}_{1y}\hat{I}_{2x}$  transferred back to observable anti-phase by 90°(*x*) pulse

# Generation and detection of multiple-quantum coherence

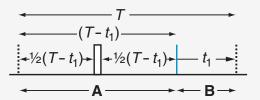
#### Typical MQC sequence



- anti-phase generated during spin echo A
- MQC generated by pulse B
- evolution
- anti-phase regenerated by pulse C; could add a further spin echo to re-phase

Generation and detection of multiple-quantum coherence 37

#### Constant time (CT) pulse sequence element

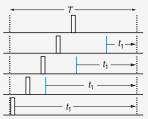


- a way of suppressing the splittings in an *indirect* dimension due to *homonuclear* coupling
- the time *T* is **fixed**, but the position of the 180° pulse changes with  $t_1$
- coupling evolves for the entire time T which, as it is constant, means that the signal is not modulated by the coupling
- offset refocused over period A, but evolves over period B (= t<sub>1</sub>), so signal is modulated by offset

# Constant time sequences

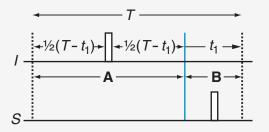
Constant time sequences 38

### CT pulse sequence element - in action



- 180° pulse moves backwards as t<sub>1</sub> increases
- problems:
  - relative amounts of in-phase and anti-phase at end of sequence depend on the size of the couplings and the time T
  - 2. it may be difficult to find a value of *T* which gives reasonable amounts of the required terms
  - 3. the maximum value of  $t_1$  is limited by T
  - 4. signal relaxes for entire time *T*, even when  $t_1 = 0$ : loss of intensity

#### CT pulse sequence element: heteronuclear case



- I-spin 180° pulse refocuses heteronuclear coupling over period A
- S-spin 180° pulse refocuses heteronuclear coupling over period B (t<sub>1</sub>)
- can re-introduce modulation due to heteronuclear coupling by displacing the S-spin pulse from the centre of period B

Constant time sequences 41

#### Isotropic mixing

a specially designed pulse sequence (e.g. DIPSI) can, over a range of offsets, generate the effective Hamiltonian

$$\hat{H}_{\rm iso} = \sum_{\rm all \ pairs \ i,j} 2\pi J_{ij} \, \hat{\mathbf{I}}_i \, . \, \hat{\mathbf{I}}_j$$

- this is the full version of the Hamiltonian for coupling (not truncated for weak coupling)
- $\hat{H}_{iso}$  is invariant to rotations hence described as *isotropic*
- DIPSI involves a continuous train of pulses with variable flip angles and phases; issue over power deposition

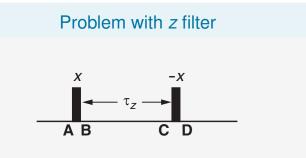
# Isotropic mixing (TOCSY)

Isotropic mixing (TOCSY) 42

#### Isotropic mixing

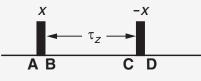
- the effect of *Ĥ*<sub>iso</sub> is to transfer magnetization (along x, y or z) from one spin to any other spin connected by an unbroken chain of couplings
- ► rate of transfer depends on the size of the coupling constants; for a two-spin system transfer goes as  $\sin^2(\pi J_{12}\tau)$
- ► transfer also results in generation of anti-phase terms from  $\hat{I}_{1x}$  or  $\hat{I}_{1y}$ , and zero-quantum coherence from  $\hat{I}_{1z}$
- need to 'clean up' the transfer e.g. using a z-filter

# **EXAMPLE 1 CALC CA**



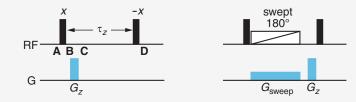
- some anti-phase terms at A are transferred to zero-quantum coherence (ZQC) at point B
- ZQC is not distinguishable from z-magnetization by phase cycling or gradient pulses: it is not suppressed, therefore
- ZQC at C becomes anti-phase magnetization at D, making z-filter ineffective

#### Problem with *z* filter: possible solution



- > ZQC evolves for time  $\tau_z$ , thus acquiring a phase
- co-addition of the results of experiments with *different* τ<sub>z</sub> values will result in partial cancellation of contributions arising from ZQC
- τ<sub>z</sub> needs to range up to a value comparable with 1/(2 × zero-quantum frequency); difficult to arrange for a complex spin system
- repetition with different  $\tau_z$  values is time consuming

#### z filter with swept gradient

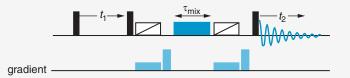


- use gradient  $G_z$  to dephase all but *z*-magnetization and ZQC
- use weak gradient in combination with swept-frequency 180° pulse to suppress ZQC (see Chapter 11, Section 11.15.2)
- one-shot z-filter: no phase cycling or repetition needed

z-filters 49

# Gradient echoes

#### TOCSY with double *z* filter



- isotropic mixing embedded in z-filter
- selection of z-magnetization before and after mixing
- ensures that only y-magnetization present before second 90° pulse and after third 90° pulse contributes to spectrum
- gives in-phase multiplets with absorption-mode lineshapes

z-filters 50

#### Field gradient pulses

- normally we try to make the B<sub>0</sub> field as homogeneous as possible ... but it can be advantageous to introduce controlled inhomogeneity
- a small coil, in the probe, generates a small field which varies linearly along z: a field gradient
- can control the *size* of the gradient by varying the current, and the *sign* by altering the direction in which the current flows
- can also control the duration of the gradient

#### Defocusing and refocusing



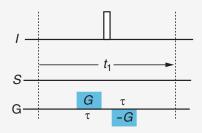
- during first gradient pulse coherence (e.g. transverse magnetization) is dephased
- extent of dephasing depends on the coherence order *p*, the duration of the gradient *τ* and its strength *G*
- after RF pulse, the coherence can be re-phased by applying a second gradient; refocusing condition:

$$\frac{G_1\tau_1}{G_2\tau_2} = -\frac{p_2}{p_1}$$

▶  $p_1 \rightarrow p_2$  pathway refocused; (hopefully) others remain dephased and so are not observed

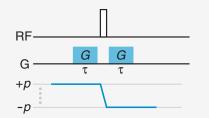
Gradient echoes 53

#### 'Cleaning up' 180° pulses in heteronuclear experiments



- coherence on S but not on I: role of 180° pulse is to invert  $\hat{I}_z$
- if pulse is imperfect may also generate transverse magnetization: second gradient dephases this
- coherence on S dephased by first gradient and rephased by second

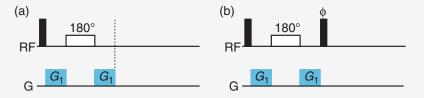
#### Refocusing pulses



- ▶ an ideal 180° pulse causes  $p \rightarrow -p$
- selected, for all p, by a pair of equal gradients
- if pulse is imperfect, gradient pair 'cleans up' any unwanted transfers
- this gradient echo is simple and convenient

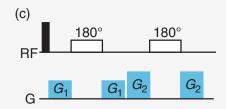
Gradient echoes 54

# Selective excitation with the aid of gradients



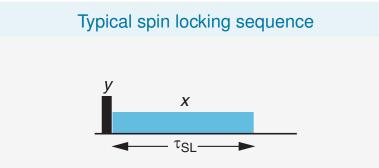
- ▶ 180° pulse is selective
- only the magn. from those spins which experience the selective pulse as a refocusing pulse will be refocused by second gradient
- everything else remains defocused: very clean excitation
- can add extra 90° pulse to flip magnetization onto -z: gives selective inversion

#### Double pulsed field gradient spin echo



- double pulsed field gradient spin echo (DPFGSE)
- only the magn. from those spins which experience both selective pulses as refocusing pulses will be excited
- advantage over single spin echo is that the phase is constant over the excited bandwidth
- two gradient pairs must be independent

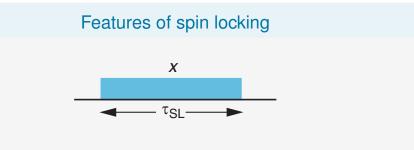
Gradient echoes 57



- non-selective pulse puts magnetization along x
- then apply a strong RF field along x
- if the RF field strength is greater than typical offsets then evolution due to offsets is suppressed and the magnetization remains 'locked' along x

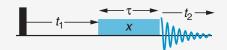


Spin locking 58



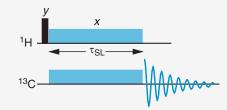
- magnetization not along the spin-lock axis likely to be dephased due to inhomogeneity of RF field
- result is a selection of just the x-magnetization
- if RF field is not large compared to the offset, then the spin-lock axis tilts up in the xz-plane (aligned with the effective field)
- heating of the sample and/or damage to the probe limits the RF power that can be used

#### **Applications: ROESY**



- ROESY: detection of cross relaxation between transverse magnetization on different spins i.e. transverse NOE
- useful in cases where conventional NOE is zero
- can also probe relaxation dispersion and chemical exchange by measuring decay of spin-locked magnetization as function of the spin-locking field strength

#### Applications: cross-polarization in solids



- Hartmann–Hahn cross polarization in solids via dipolar coupling
- transfer of magnetization from abundant <sup>1</sup>H to low-abundance <sup>13</sup>C: need to match field strengths according to  $\gamma_I \omega_{1,I} = \gamma_S \omega_{1,S}$

Spin locking 62

used for: (a) sensitivity enhancement; (b) transfer of magnetization in multiple-pulse experiments

Spin locking 61

55<sup>th</sup> Experimental Nuclear Magnetic Resonance Conference

Boston, 2014

# The Basic Building Blocks of NMR Pulse Sequences

# The End

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